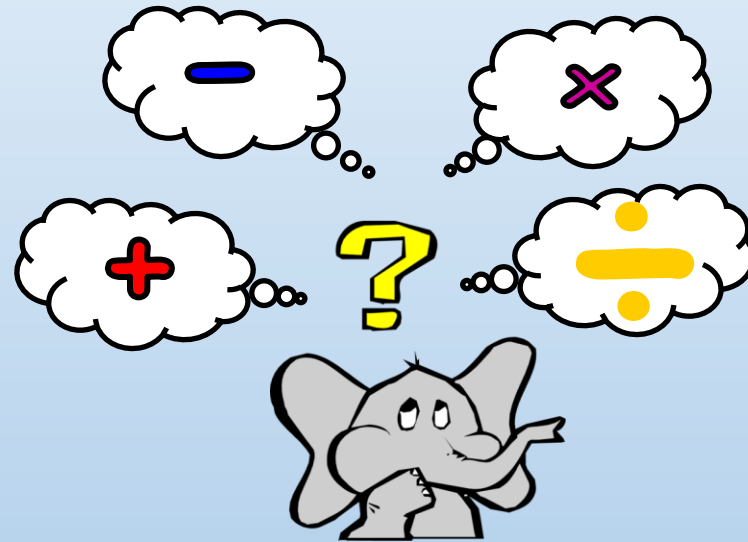


# Mathematics at Wickham Common



Workshop for parents

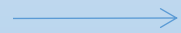


# By Key Stage 2

- Choosing a calculation method:

Before pupils opt for a written method they should first consider these steps:

Can I do it in my head using a mental strategy?



Could I use some jottings to help me?



Should I use a formal written method to work it out?

# NCETM principles

- *Develop children's fluency with basic number facts*
- *Develop children's fluency in mental calculation*
- *Develop children's understanding of the = symbol*
- *Teach inequality alongside teaching equality*
- *Use empty box problems*
- *Use intelligent practice*
- *Expose mathematical structure and work systematically*
- *Move between the concrete, pictorial and the abstract (CPA)*
- *Contextualise the mathematics*

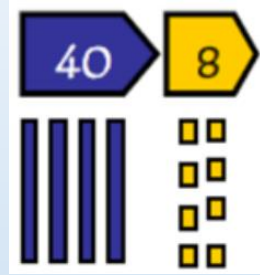
# Potential issues

- Confidence (including parents!)
- Language
- Abstract
- Method without understanding
- Reading for reasoning

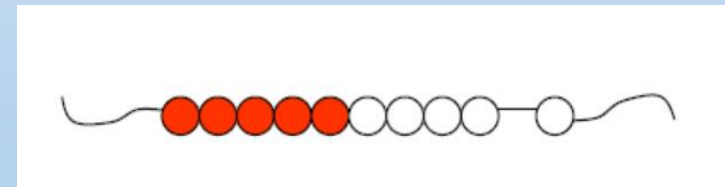
# Addition

## Concrete resources:

- 100 square
- Number lines
- Bead strings
- Straws
- Dienes
- Place value cards
- Place value dice
- Place value counters
- Numicon



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



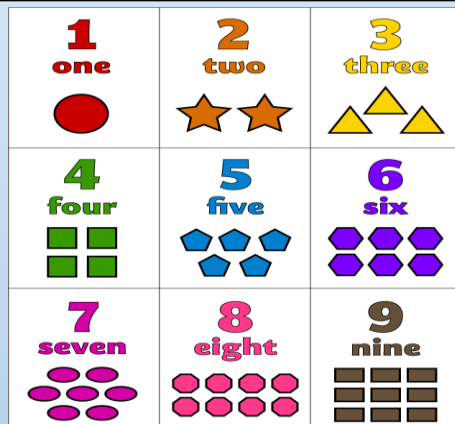
sum      addition      total  
make  
and      +      more  
add      plus  
altogether      increase

# Addition: Reception

Early learning goals:

- ✓ Count reliably with numbers from 1 to 20, place them in order.
- ✓ Say which number is one more than a given number.
- ✓ Using quantities and objects, they add two single-digit numbers and count on to find the answer.

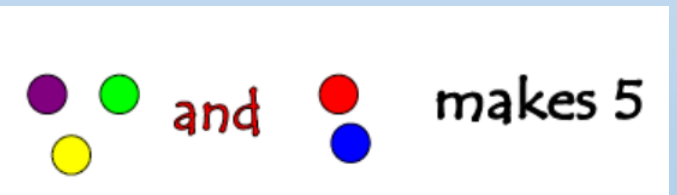
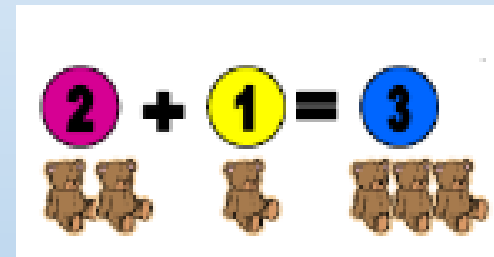
Recognise numbers up to 20 and understand the meaning of each number by recognising and knowing their clusters



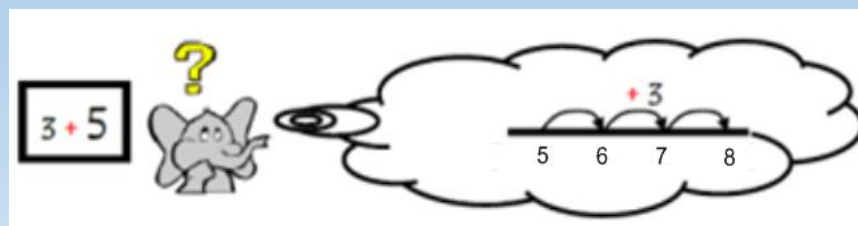
Count on in ones and say which number is one more than a given number using a number line or number track to 20.



Begin to relate addition to combining two groups of objects using practical resources, role play, stories and songs.



Know that counting on is a strategy for addition. Use numbered number lines to 20.



# Addition: Year 1

Year 1 statutory requirements :

- ✓ Count to and across 100, forwards beginning with 0 or 1, or from any given number.
- ✓ Given a number, identify one more.
- ✓ Read, write and interpret mathematical statements involving addition (+), and equals (=) signs.
- ✓ Represent and use number bonds and related subtraction facts within 20
- ✓ Add one-digit and two-digit numbers to 20, including zero.
- ✓ Solve one-step problems that involve addition using concrete objects and pictorial representations, and missing number problems.

Identify and represent numbers using objects and pictorial representations (multiple representations)



Memorise and reason with number bonds to 10 and 20 in several forms.

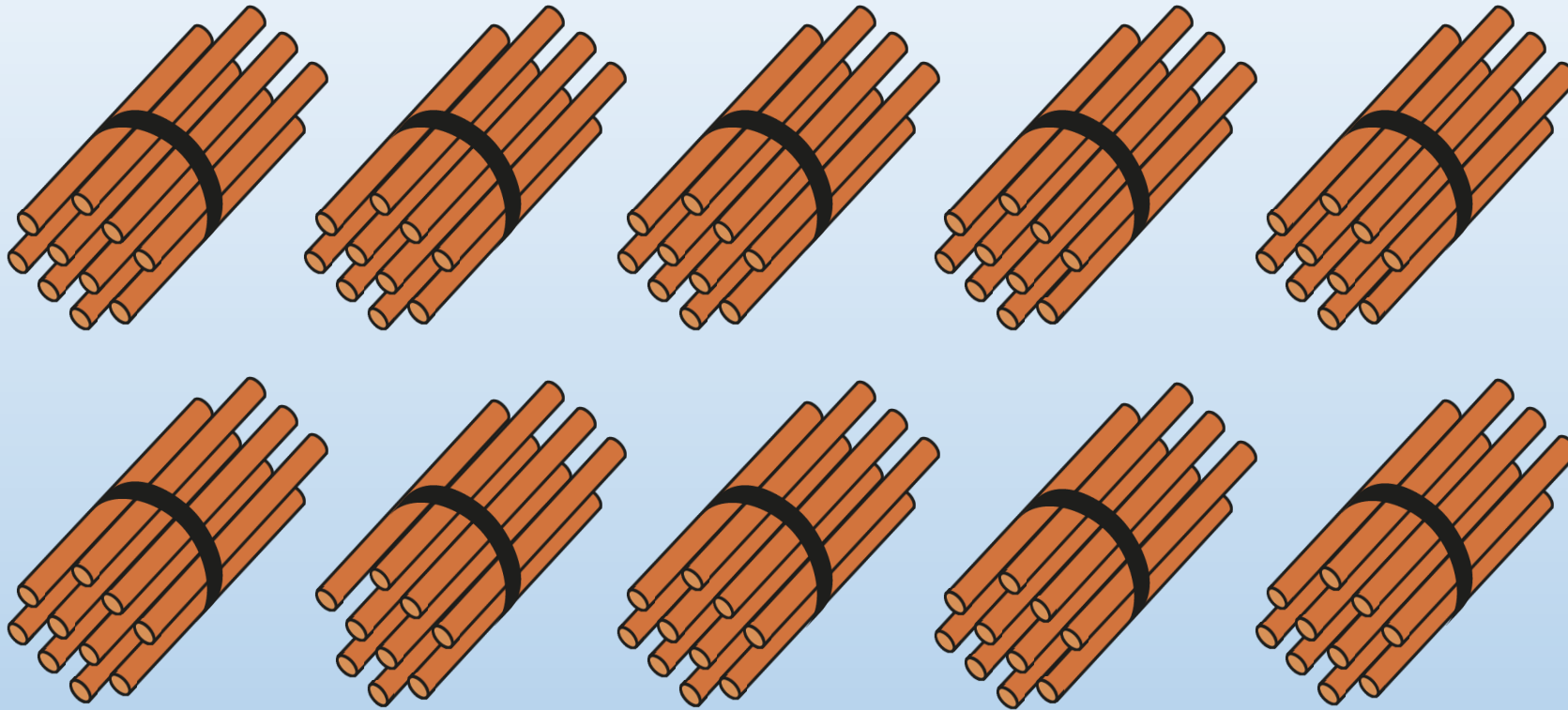


Count on in ones to and across 100 and find one more than a given number.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

	$6 + 4 = 10$ $4 + 6 = 10$ $10 - 4 = 6$ $10 - 6 = 4$		$6 + 4 = 10$ $4 + 6 = 10$ $10 - 4 = 6$ $10 - 6 = 4$	<table border="1"> <tbody> <tr><td colspan="2">10</td></tr> <tr><td>6</td><td>4</td></tr> </tbody> </table>	10		6	4	$6 + 4 = 10$ $4 + 6 = 10$ $10 - 4 = 6$ $10 - 6 = 4$
10									
6	4								
Tens Frame		Part Whole Model		Bar Model					

## 1NPV-1 Count forwards and backwards within 100



- Begin by using real straws to count and bundle together in groups of 10.

x

*Seven, eight, nine, ten, eleven, twelve... twenty, twenty-one, twenty-two...*

*Seven, eight, nine, ten, one-ten, one-ten-one, one-ten-two... two-tens, two-tens-one, two-tens-two...*

- Can you count in ones between 1 and 100, both forwards and backwards?
- Can you start your count from different numbers?
- Can you say the number of straws each time a bundle is tied up? Louder!
- Are you saying the 'teen numbers' clearly?
- Can you say the count in two ways?



# 1NPV-1 Count forwards and backwards within 100

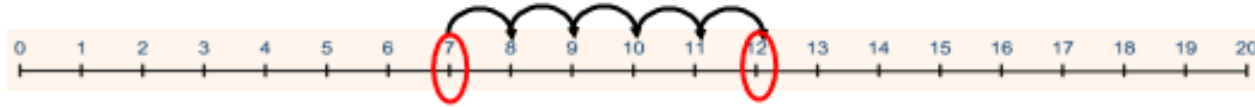
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
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61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

- Can you count forwards and backwards between 1 and 100, starting in different places on the 100 square?
- Can you say the ‘teen’ part of these numbers a little louder? *Thirteen, fourteen, fifteen...*
- Can you say the numbers which come after these numbers: 19..., 29..., 39..., 99...? Say them loudly and clearly: *twenty, thirty, forty...*
- Can you say the numbers which come before these numbers: 30, 50, 70, 100?
- Where on the 100 square can you see the counting numbers which come before 21, 31, 41...?



# Addition: Year 1

Use concrete resources and a number line to support the addition of numbers. Know and use strategy of finding the larger number, and counting on in ones from this number.



1 digit + 1 digit

$$7 + 5 = 12$$



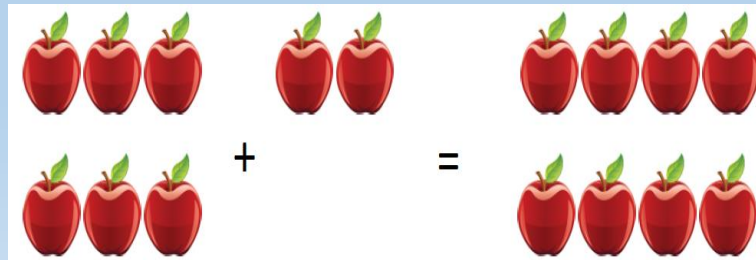
2 digit + 1 digit

$$18 + 5 = 23$$

Begin to use the + and = signs to write calculations in a number sentence.

Solve one-step problems using concrete objects and pictorial representations.

Tom picks 6 apples and Raj picks 2 apples.  
How many apples do they have altogether?

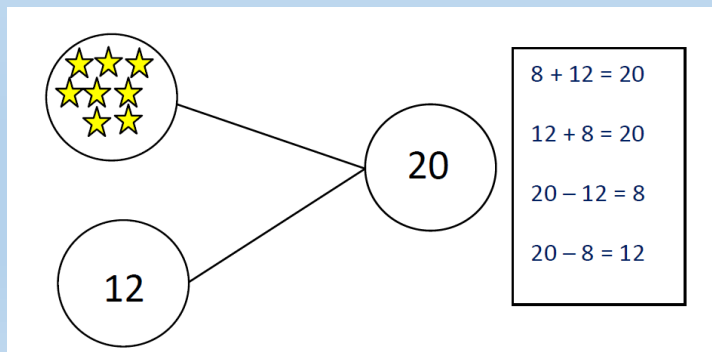


# Addition: Year 2

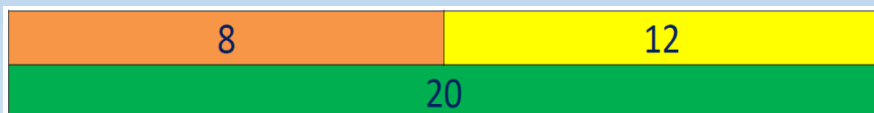
Year 2 statutory requirements :

- ✓ Recall and use addition and subtraction facts to 20 fluently, and derive and use related facts to 100.
- ✓ Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.
- ✓ Add numbers using concrete objects, pictorial representations, and mentally, including:
  - a two-digit number and ones
  - a two-digit number and tens
  - two two-digit numbers
  - adding three one-digit numbers.
- ✓ Solve problems with addition including those involving numbers, quantities and measures.

Memorise and reason with number facts to 20 in several forms.

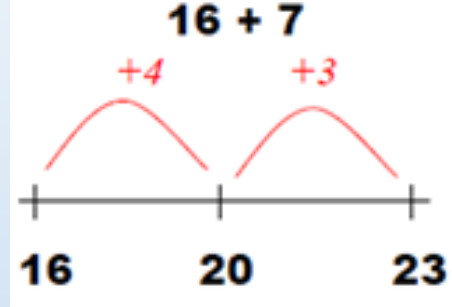


Partition two 2-digit numbers using a variety of models and images.

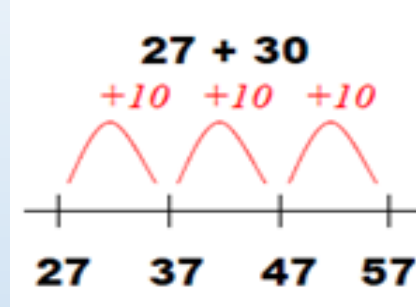


# Addition: Year 2

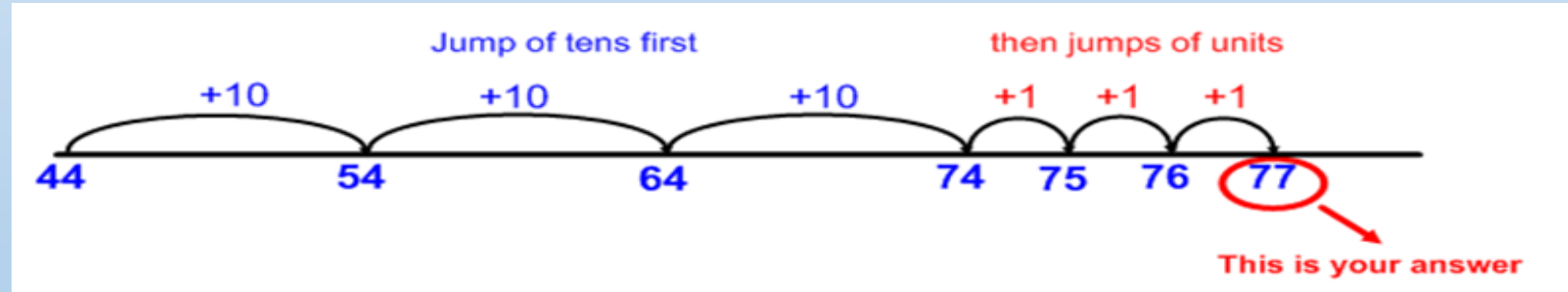
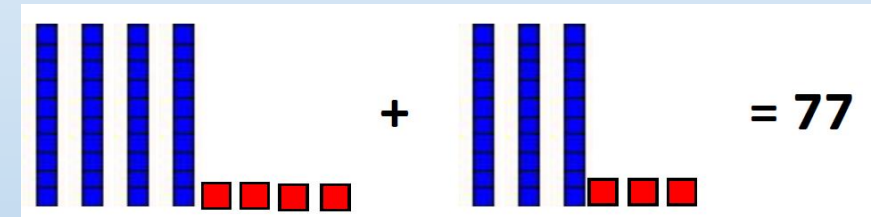
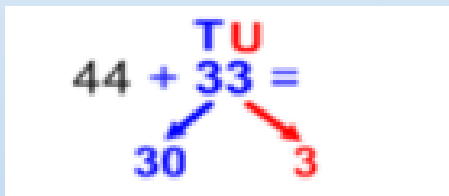
Add 2 digit number and ones



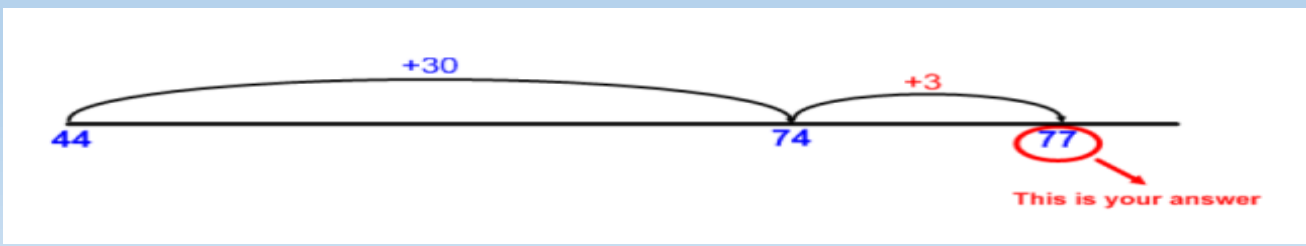
Add 2 digit number and tens



Use partitioning to add two 2-digit numbers using concrete resources and/or a numbered number line and then progressing to an empty number line.



As children gain confidence with adding on tens and ones, they should be taught to combine the jumps on an empty number line.



# Addition: Year 3

Year 3 statutory requirements :

- Find 10 or 100 more than a given number.
- Recognise the place value of each digit in a three-digit number (hundreds, tens, ones).
- Add numbers with up to three digits, using formal written methods of columnar addition.

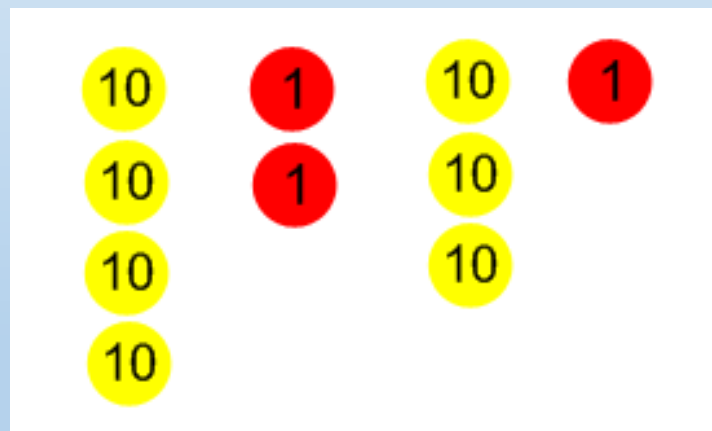
Use expanded column method with place value resources to support the conceptual understanding of adding numbers up to three digits **with no carrying**.

$$42 + 31 = 73$$

$$40 + 2$$

$$\underline{30 + 1}$$

$$\underline{70 + 3}$$



OR

Tens	Ones
70	3

# Addition: Year 3

Progress to using the expanded column method with place value resources to support the conceptual understanding of adding numbers up to three digits *with carrying*.

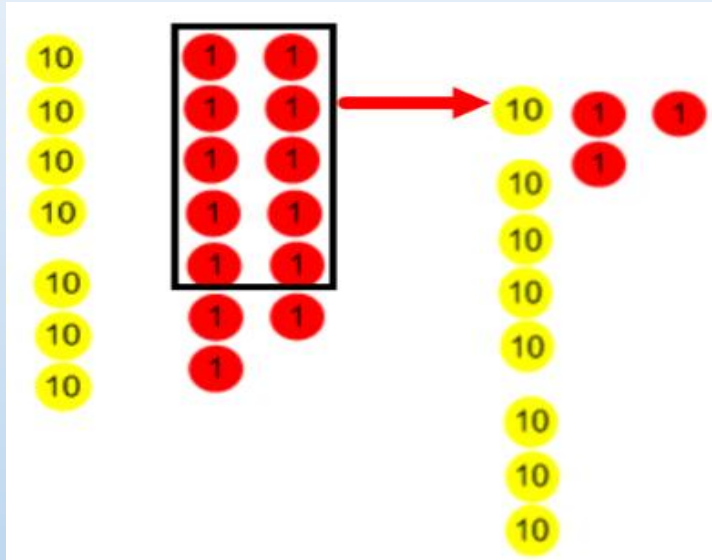
$$47 + 36 = 83$$

$$40 + 7$$

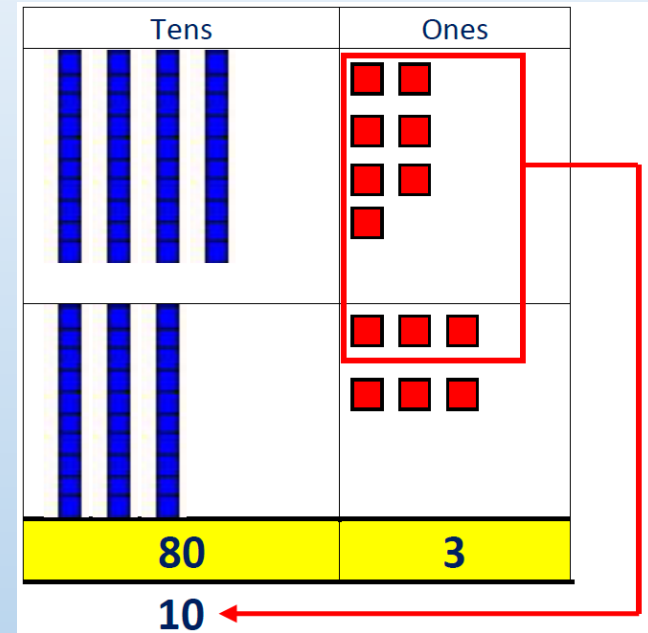
$$30 + 6$$

$$80 + 3$$

$$10$$



OR



Extend to using the expanded column method to add three digit numbers + three digit numbers *with carrying*.

$$367 + 185 = 552$$

$$300 + 60 + 7$$

$$100 + 80 + 5$$

$$500 + 50 + 2$$

$$100 \quad 10$$

**Note:** The carried ten or carried hundred is just as important as any other number, therefore, it should be written as clear and as large as any other number, and placed at the **bottom** of the column in which it is to be added.

# Addition: Year 4

Year 4 statutory requirements :

- Find 1000 more than a given number.
- Add numbers with up to 4 digits using the formal written methods of columnar addition where appropriate.
- Solve addition two-step problems in contexts, deciding which operations and methods to use and why,

Build on learning from Year 3 and model how expanded method links to compact column addition method.

$$\begin{array}{r} 40 + 7 \\ \underline{30 + 6} \\ \underline{80 + 3} \\ 10 \end{array} \quad \longrightarrow \quad \begin{array}{r} 47 \\ +36 \\ \underline{\phantom{00}83} \\ 1 \end{array}$$

$$\begin{array}{r} 300 + 60 + 7 \\ \underline{100 + 80 + 5} \\ \underline{500 + 50 + 2} \\ 100 \quad 10 \end{array} \quad \longrightarrow \quad \begin{array}{r} 367 \\ +185 \\ \underline{\phantom{00}552} \\ 11 \end{array}$$

**Note:** The carried ten or carried hundred is just as important as any other number, therefore, it should be written as clear and as large as any other number, and placed at the **bottom** of the column in which it is to be added.

By the end of year 4, pupils should be adding numbers up to 4 digits using compact column addition method.

$$\begin{array}{r} 5271 \\ +2357 \\ \underline{\phantom{00}7628} \\ 1 \end{array}$$

# Addition: Year 5 & 6

Year 5 statutory requirements :

- Add whole numbers with more than 4 digits using formal written methods of columnar addition.
- Add numbers mentally, with increasingly large numbers.
- Solve addition multi-step problems in contexts, deciding which operations and methods to use and why.
- Solve problems involving numbers up to three decimal places

Year 6 statutory requirements :

- Pupils are expected to solve more complex addition and subtraction problems

In year 5 and 6 pupils should be adding numbers using compact column addition method. **Note:** The carried ten, hundred, thousand is just as important as any other number, therefore, it should be written as clear and as large as any other number, and placed at the **bottom** of the column in which it is to be added.

$$\begin{array}{r} 46892 \\ + 32758 \\ \hline 79650 \\ \hline 111 \end{array}$$

When adding decimals, it is essential that the decimal point does not move and kept in line.

Where necessary, a zero should be added as a **place holder**.

$$12.5 + 23.7$$

$$\begin{array}{r} 12.5 \\ + 23.7 \\ \hline 36.2 \\ \hline 1 \end{array}$$

$$34.5 + 27.43$$

$$\begin{array}{r} 34.50 \\ + 27.43 \\ \hline 61.93 \\ \hline 1 \end{array}$$

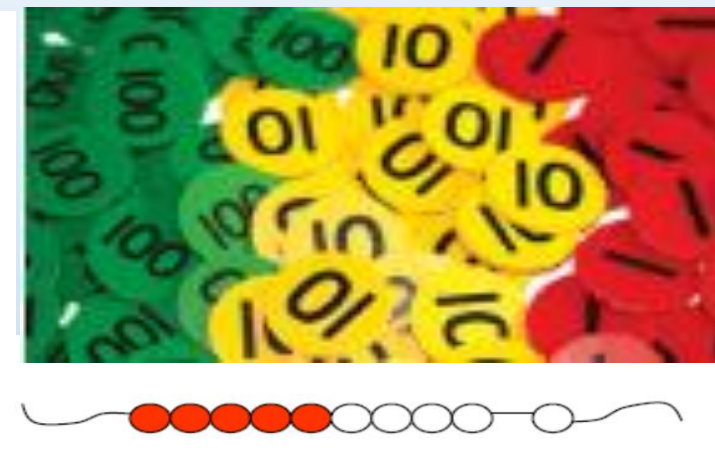
# Subtraction

## Concrete resources:

- 100 square
- Number lines
- Bead strings
- Straws
- Dienes
- Counting stick
- Place value dice
- Place value cards
- Place value counters



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



subtract  
count on      count back  
fewer      —      less  
take away      minus  
                         difference



# Subtraction: Reception

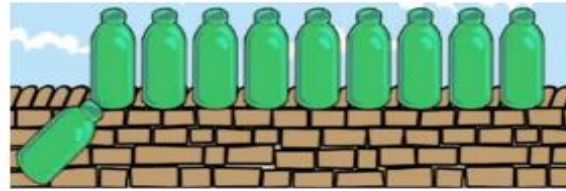
Early learning goals:

- ✓ Say which number is one less than a given number.
- ✓ Using quantities and objects, they subtract two single-digit numbers and count back to find the answer.

Say which number is one less than a given number using a number line or number track to 20.



Begin to count backwards in familiar contexts such as number rhymes or stories.

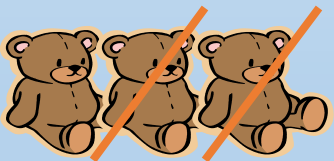


10 Green Bottles sitting on the wall ...

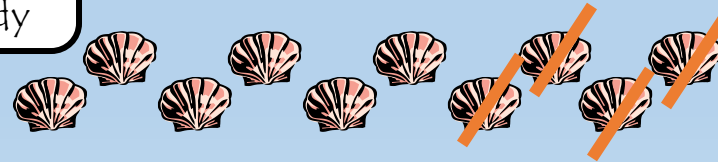


5 little ducks went swimming one day...

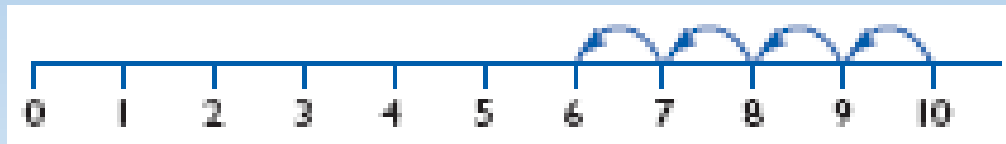
Begin to relate subtraction to 'taking away' using concrete objects and role play.



Three teddies **take away** two teddies leaves one teddy



If I **take away** four shells there are six left



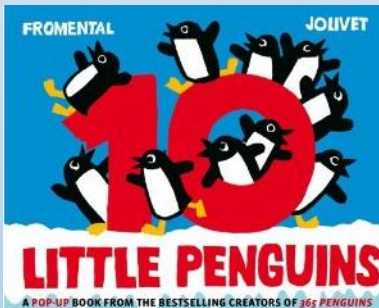
Count backwards along a number line to 'take away'

# Subtraction: Year 1

Year 1 statutory requirements:


- ✓ Say which number is one less than a given number.
- ✓ Represent and use number bonds and related subtraction facts within 20.
- ✓ Read, write and interpret mathematical statements involving subtraction (-) and equals (=) signs.
- ✓ Subtract one-digit and two-digit numbers to 20, including zero.
- ✓ Solve one-step problems that involve subtraction using concrete objects and pictorial representations, and missing number problems.

Understand subtraction as take away. Use practical resources, pictorial representations, role play, stories and rhymes.



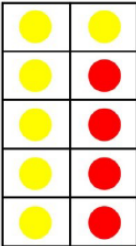
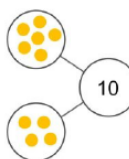
Use number bonds and related subtraction facts within 20.

$$16 - \square = 10$$

$$20 - \square = 15$$


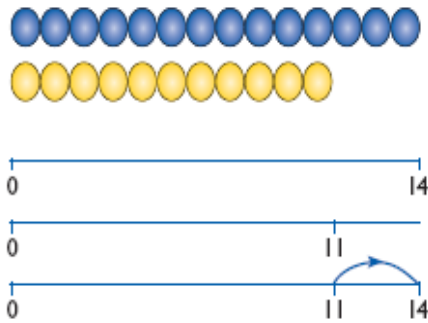
Count back in ones and find one less than a given number.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
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10						
6	4					
Tens Frame	Part Whole Model	Bar Model				

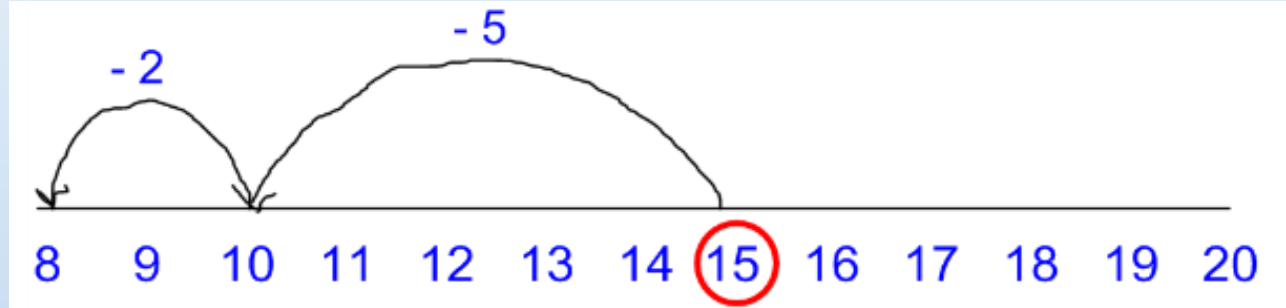
# Subtraction: Year 1

**Counting on** should only be used when the language used is 'find the difference', 'difference between' and 'distance between'.



The difference between 11 and 14 is 3.  
 $14 - 11 = 3$   
 $11 + \square = 14$

Use number line to support the subtraction of numbers. Know and use strategy of **counting back** to subtract one-digit and two-digit numbers to 20.



$$15 - 7 = 8$$

Begin to use the - and = signs to write calculations in a number sentence.

Solve one-step problems using concrete objects and pictorial representations.

Dan has 12 football stickers.  
He gives 4 to Ben.  
How many stickers does he have left?



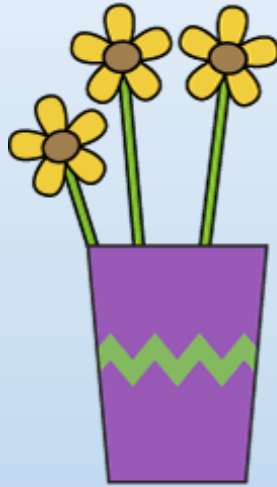
12

- 4 =

8

1NF-1 Fluently add and subtract within 10 – adding and subtracting 1, difference of 1

First



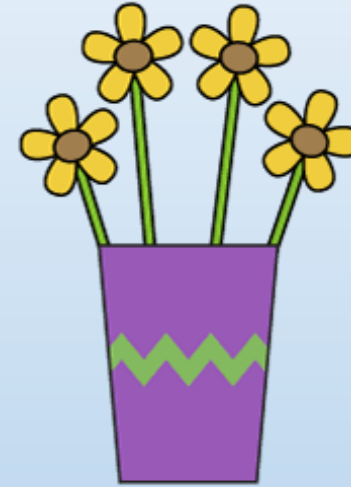
3

Then



+ 1

Now



4



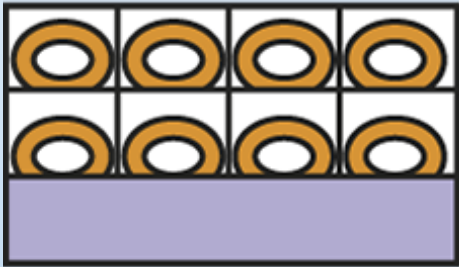
$$3 + 1 = 4$$

*I know that one more than 3 is 4, so I know that 3 plus 1 is 4.*



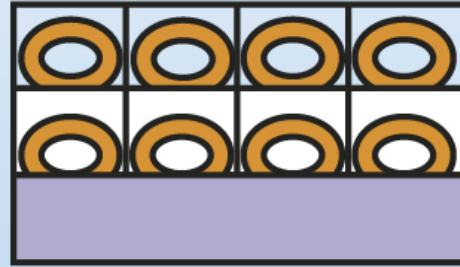
# 1NF-1 Fluently add and subtract within 10 – adding and subtracting 1, difference of 1

First



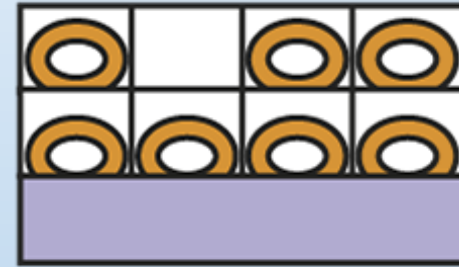
8

Then



- 1

Now



7



$$8 - 1 = 7$$

*I know that one less than 8 is 7, so I know that 8 minus 1 is 7.*

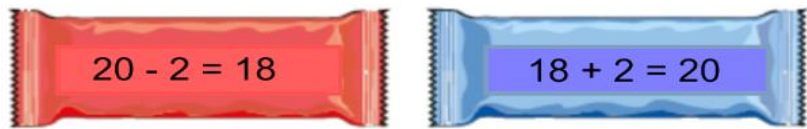
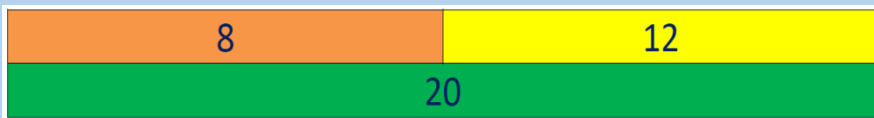
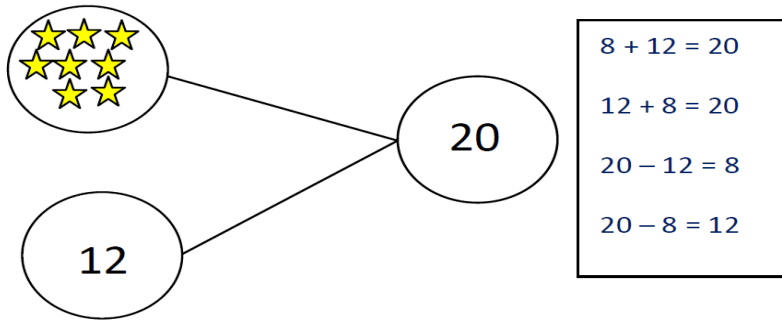


# Subtraction: Year 2

Year 2 statutory requirements:

- Recall and use subtraction facts to 20 fluently, and derive and use related facts to 100.
- Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.
- Subtract numbers using concrete objects, pictorial representations, and mentally, including:
  - a two-digit number and ones
  - a two-digit number and tens
  - two two-digit numbers
  - adding three one-digit numbers.

Memorise and reason with number facts to 20 in several forms.

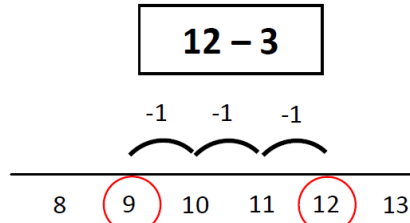


Partition two 2-digit numbers using a variety of models and images.

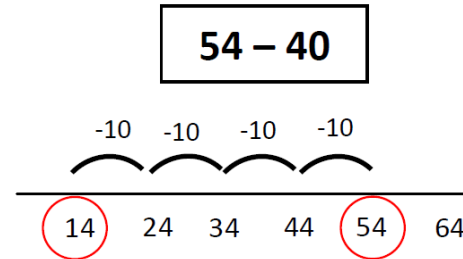


# Subtraction: Year 2

Subtract 2 digit and ones



Subtract 2 digit and tens



Use partitioning to subtract two 2-digit numbers using concrete resources and/or a numbered number line and then progressing to an empty number line.

$$36 - 12 = 24$$

A diagram showing the partitioning of 36. A blue arrow points from 36 down to 10, and a red arrow points from 36 down to 2.

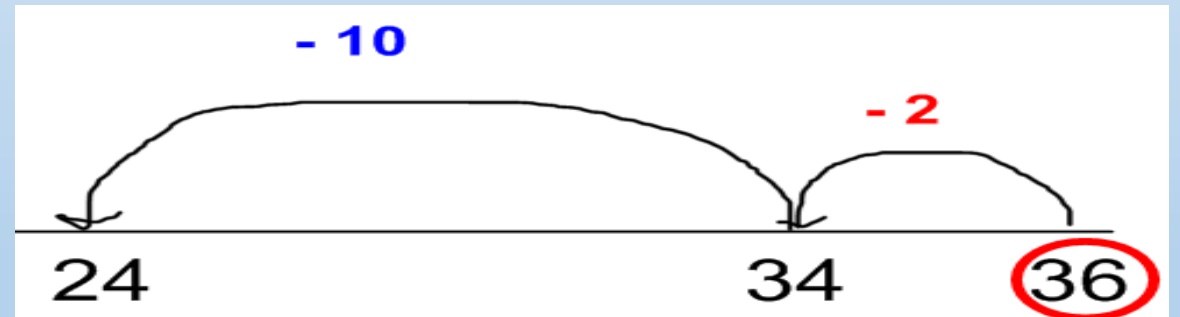


$$36 - 12$$

=

$$24$$

OR



# Subtraction: Year 3

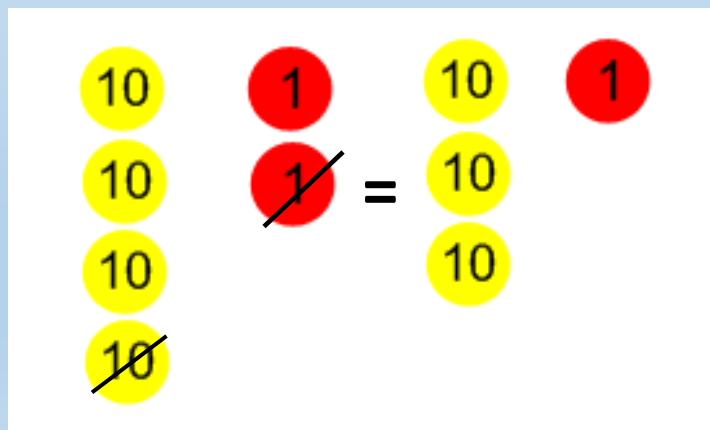
Year 3 statutory requirement:

- Find 10 or 100 less than a given number.
- Recognise the place value of each digit in a three-digit number (hundreds, tens, ones).
- Subtract numbers with up to three digits, using formal written methods of column subtraction.
- Subtract numbers mentally, including:
  - A three-digit number and ones
  - A three-digit number and tens
  - A three-digit number and hundreds.

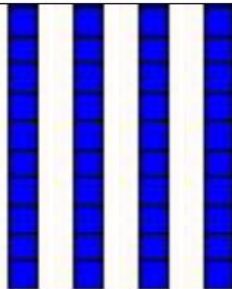
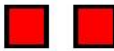
Use expanded column method with place value resources to support the conceptual understanding of subtracting numbers with up to three digits **with no exchanging**.

$$42 - 11 = 31$$

$$\begin{array}{r} 40 + 2 \\ - 10 + 1 \\ \hline 30 + 1 \end{array}$$



OR

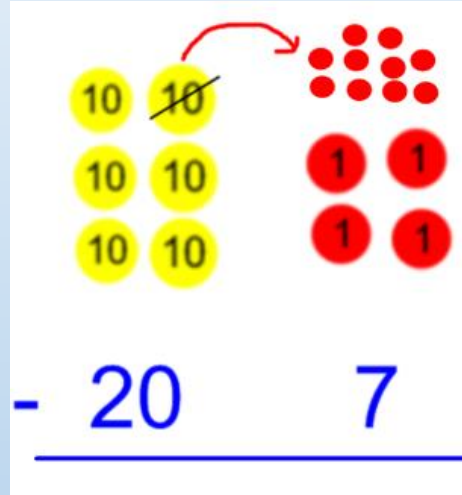
Tens	Ones
	
- 10	- 1
30	1

# Subtraction: Year 3

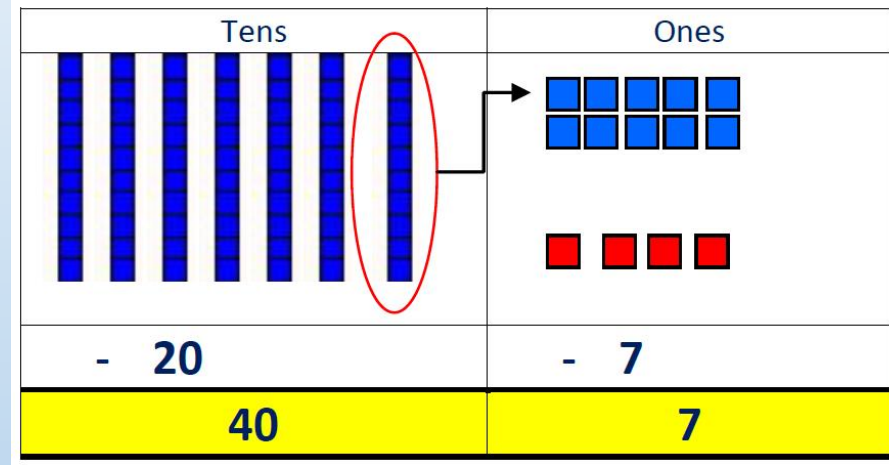
Progress to using the expanded column method with place value resources to support the conceptual understanding of subtracting numbers with up to three digits *with exchanging tens and/or hundreds*.

$$74 - 27 = 47$$

$$\begin{array}{r}
 60 + 14 \\
 \cancel{70} + \cancel{4} \\
 - 20 + 7 \\
 \hline
 40 + 7 \\
 \hline
 \end{array}$$



OR



In this example to subtract 7 ones from 4 ones we need to **exchange** a ten for ten ones. We now can subtract 7 ones from 14 ones.

Extend to using the expanded column method to subtract three digit numbers from three digit numbers.

$$537 - 254 = 283$$

$$\begin{array}{r}
 400 + 130 \\
 \cancel{500} + \cancel{30} + 7 \\
 - 200 + 50 + 4 \\
 \hline
 200 + 80 + 3 \\
 \hline
 \end{array}$$

**Note:** The exchanged ten or hundred is just as important as any other number, therefore, it should be written as clear and as large as any other number, and placed at the **top** of the column which has been adjusted.

# Subtraction: Year 4

Year 4 statutory requirements:

- Find 1000 less than a given number.
- Subtract numbers with up to four digits, using formal written methods of columnar subtraction where appropriate.
- Solve subtraction two-step problems in contexts, deciding which operations and methods to use and why.

Build on learning from Year 3 and model how expanded method links to compact column subtraction method.

$$\begin{array}{r}
 60 + 14 \\
 \cancel{70} + \cancel{4} \\
 - \quad \underline{20 + 7} \\
 \underline{40 + 7}
 \end{array}$$



$$\begin{array}{r}
 6 \\
 \cancel{7}^1 4 \\
 \underline{27} \\
 \underline{47}
 \end{array}$$

$$\begin{array}{r}
 400 + 130 \\
 \cancel{500} + \cancel{30} + 7 \\
 - \quad \underline{200 + 50 + 4} \\
 \underline{200 + 80 + 3}
 \end{array}$$



$$\begin{array}{r}
 4 \\
 \cancel{5}^1 \cancel{3} 7 \\
 - \quad \underline{254} \\
 \underline{283}
 \end{array}$$

By the end of year 4, pupils should be subtracting numbers up to 4 digits using compact column subtraction method.

$$\begin{array}{r}
 \phantom{-} \phantom{7} \phantom{8} \phantom{4}^3 \phantom{2} \\
 \phantom{-} \phantom{7} \phantom{8} \phantom{4}^1 \phantom{2} \\
 - \quad \underline{1829} \\
 \underline{6013}
 \end{array}$$

**Note:** The exchanged ten or hundred is just as important as any other number, therefore, it should be written as clear and as large as any other number, and placed at the **top** of the column which has been adjusted.

# Subtraction: Year 5 & 6

Year 5 statutory requirements :

- Subtract whole numbers with more than 4 digits using formal written methods of columnar subtraction.
- Subtract numbers mentally, with increasingly large numbers.
- Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why.
- Solve problems involving numbers up to three decimal places.

Year 6 statutory requirements: pupils are expected to solve more complex addition and subtraction problems

In year 5 and 6 pupils should be subtracting numbers using compact column subtraction method. **Note:** The exchanged ten or hundred is just as important as any other number. Therefore, it should be written as clear and as large as any other number, and placed at the **top** of the column which has been adjusted.

$$\begin{array}{r}
 8 \qquad \qquad \qquad 7 \\
 \cancel{9} \quad ^1 6 \quad 7 \quad \cancel{8} \quad ^1 3 \\
 - \\
 \hline
 5 \quad 8 \quad 7 \quad 3 \quad 5 \\
 \hline
 3 \quad 8 \quad 0 \quad 4 \quad 8
 \end{array}$$

When subtracting decimals, it is essential that the decimal point does not move and kept in line.

Where necessary, a zero should be added as a *place holder*.

$$\begin{array}{r}
 4 \\
 \cancel{5} \cdot ^1 3 \quad 7 \\
 - 2 \cdot 5 \quad 4 \\
 \hline
 2 \cdot 8 \quad 3
 \end{array}$$

	<del>1</del>	<del>10</del>	15	.	<del>4</del>	1	9	kg
-		3	6	.	0	8	0	kg
		6	9	.	3	3	9	kg

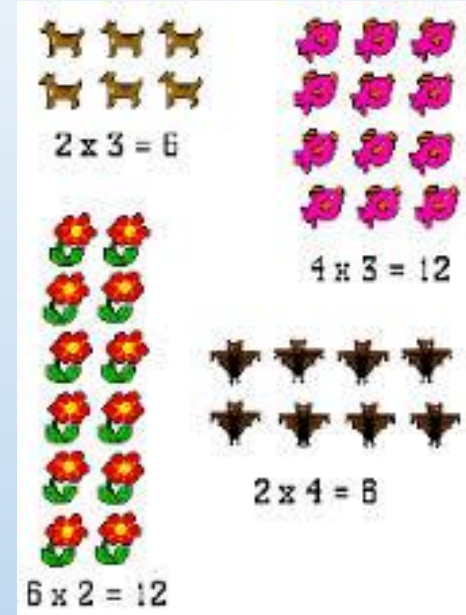
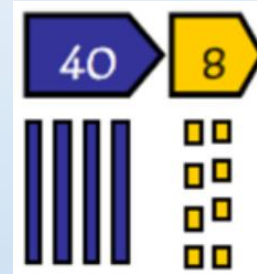
# Multiplication

## Concrete resources

- Place value counters
- Dienes
- Place value charts
- Arrays
- Multiplication squares
- 100 square
- Number lines
- Blank number lines
- Counting stick



1	2	3	4	5	6	7	8	9	10
2	4	6	8	10	12	14	16	18	20
3	6	9	12	15	18	21	24	27	30
4	8	12	16	20	24	28	32	36	40
5	10	15	20	25	30	35	40	45	50
6	12	18	24	30	36	42	48	54	60
7	14	21	28	35	42	49	56	63	70
8	16	24	32	40	48	56	64	72	80
9	18	27	36	45	54	63	72	81	90
10	20	30	40	50	60	70	80	90	100



**multiplication**      **product**  
 once, twice, three times  
**double**      **groups of**  
 repeated addition      **lots of**  
 array, row, column      **multiply**  
**times**      **multiple**

# Multiplication: Reception

Early learning goal statutory requirement:

✓They solve problems, including doubling, halving and sharing.

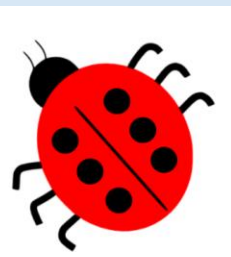
Use pictorial representations and concrete resources to double numbers to 10.



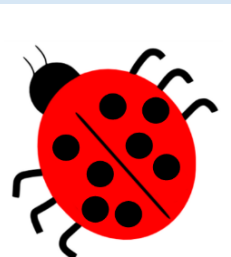
$$1 + 1 = 2$$



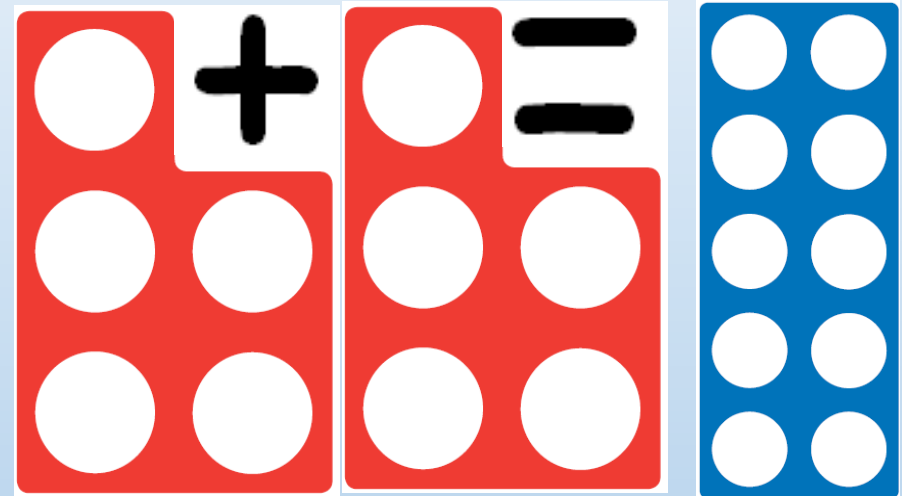
$$2 + 2 = 4$$



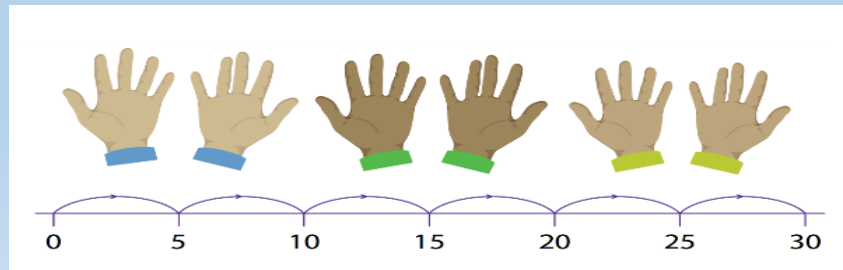
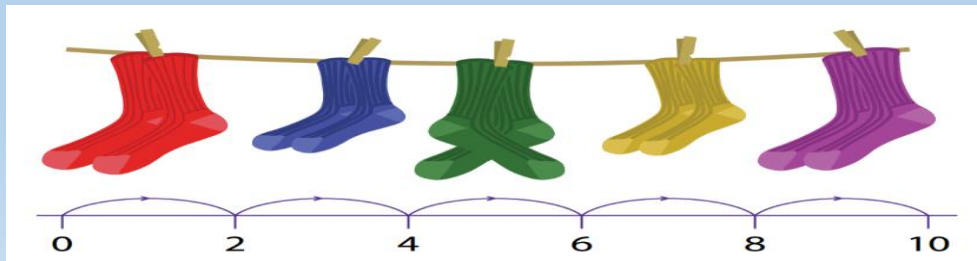
$$3 + 3 = 6$$



$$4 + 4 = 8$$



Use concrete sources, role play, stories and songs to begin counting in twos, fives and tens.

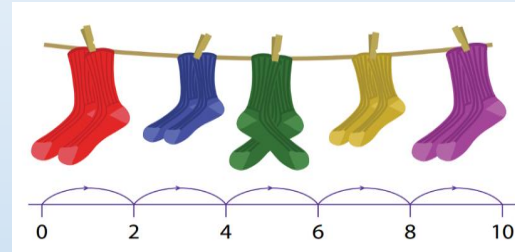
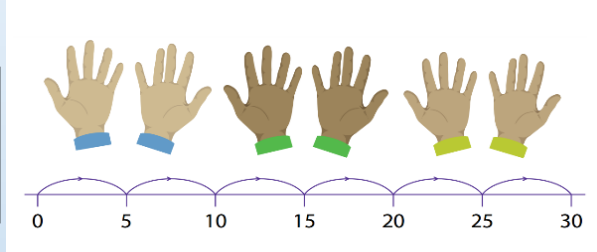


# Multiplication: Year 1

Year 1 statutory requirement:

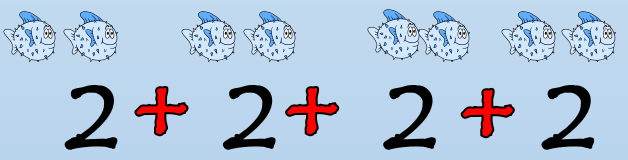
✓ Solve one-step problems involving multiplication by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

Count in twos, fives and tens using practical resources, role play, stories and songs.

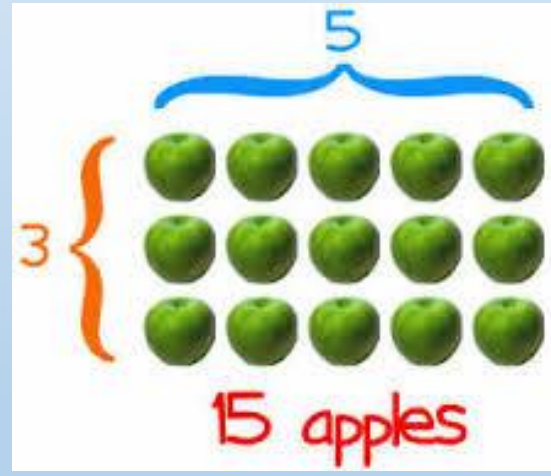


Use arrays

Understand multiplication as repeated addition – use concrete objects to support understanding.



Use pictorial representations



# Multiplication: Year 2

Year 2 statutory requirement:

- ✓ Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers.
- ✓ Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication ( $\times$ ), division ( $\div$ ) and equals ( $=$ ) signs.
- ✓ Show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot.
- ✓ Solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.

Further develop understanding multiplication as repeated addition.

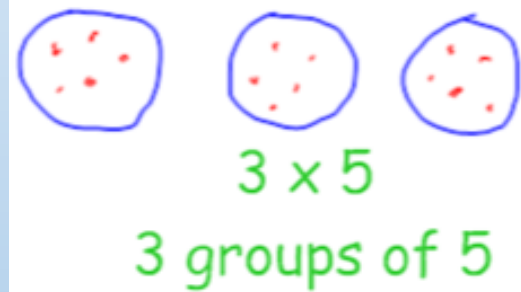


$$5 + 5 + 5$$

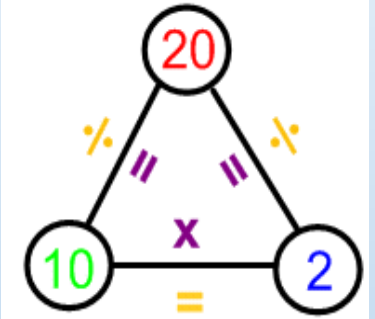
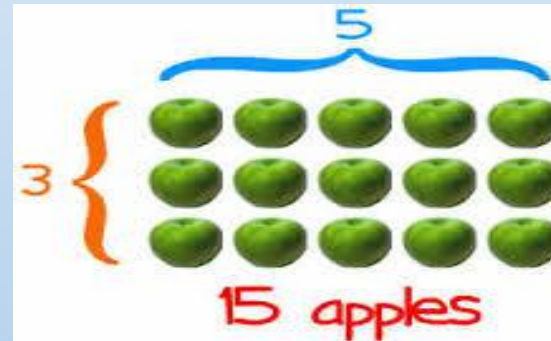
or

$$5 \times 3$$

Use pictorial representations

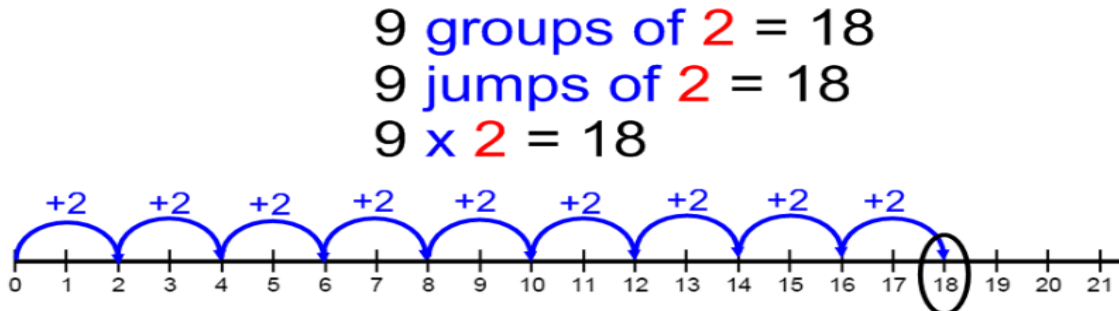


Use arrays

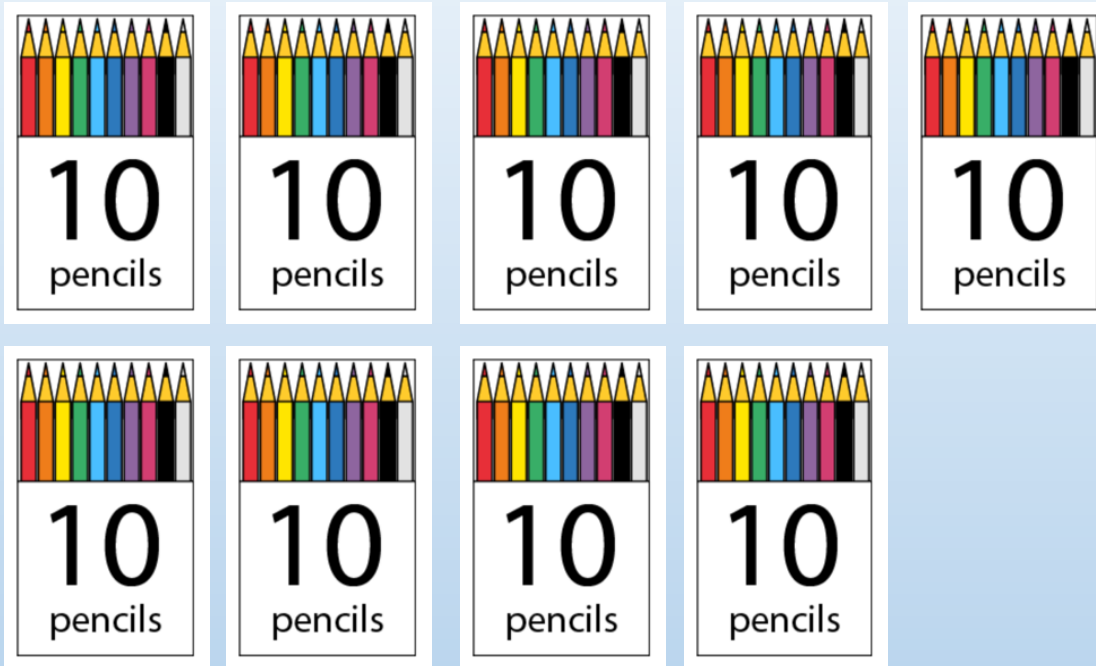


Recall multiplication and division facts for 2, 5, 10

Model and bridge link from repeated addition to solving multiplication problems using a number line.



## 2MD-1 Multiplication as repeated addition



$$9 \times 10$$



- Can you say what the expression to match the picture should be?
- What multiple do we need to skip count in to find out *how many pencils* there are *altogether*?
- If we skip count in multiples of 10, how many 10s will we need to count?
- So, 10, 20, 30, 40, 50, 60, 70, 80, 90... there are 90 pencils altogether.

*The 9 represents the number of groups.  
The 10 represents the number of pencils in each group.  
The 90 represents the total number of pencils.*



## 2MD-1 Multiplication as repeated addition



$$7 \times 2$$



- What expression can we write to match the picture?
- Can you tell me what multiple we need to skip count in to find out how many wheels there are *altogether* on the bikes?
- How many twos will you need to count?
- So, 7 times 2 is equal to \_\_\_\_\_.
- Can you say what each number in the equation means?



# Multiplication: Year 3

Year 3 statutory requirements:

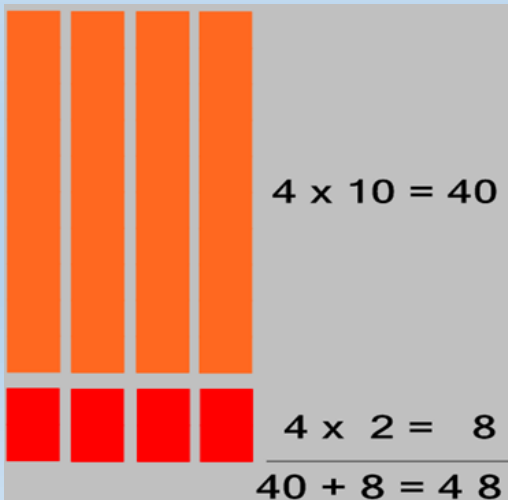
- ✓ Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables.
- ✓ Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.
- ✓ Solve problems, including missing number problems, involving multiplication including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.

Develop recall of multiplication facts (alongside inverse of the corresponding division facts).

x	3	4	8	x	4	?	?
5				?	8	6	10
6				6	24	18	30
4				?	32	24	40

Use concrete resources to develop conceptual understanding of the compact method introduced in Year 4.

$$12 \times 4 = 48$$



x	10	2
4		

OR

x	10	2
4	40	8

$$\begin{array}{r}
 10 + 2 \\
 \times \quad 4 \\
 \hline
 8 \\
 40 \\
 \hline
 48
 \end{array}$$



The yellow ribbon is 4 times as long as the red ribbon. What is its length?

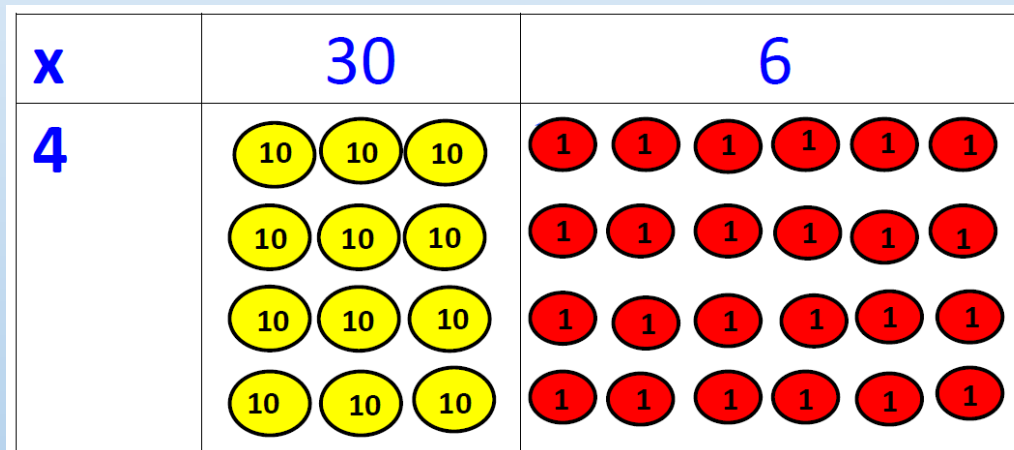
# Multiplication: Year 4

Year 4 statutory requirement:

- ✓ Recall multiplication and division facts for multiplication tables up to  $12 \times 12$
- ✓ Use place value, known and derived facts to multiply and divide mentally, including: multiply two-digit and three-digit numbers by a one-digit number using formal written layout.
- ✓ Solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects.

X	1	2	3	4	5	6	7	8	9	10	11	12
1	1	2	3	4	5	6	7	8	9	10	11	12
2	2	4	6	8	10	12	14	16	18	20	22	24
3	3	6	9	12	15	18	21	24	27	30	33	36
4	4	8	12	16	20	24	28	32	36	40	44	48
5	5	10	15	20	25	30	35	40	45	50	55	60
6	6	12	18	24	30	36	42	48	54	60	66	72
7	7	14	21	28	35	42	49	56	63	70	77	84
8	8	16	24	32	40	48	56	64	72	80	88	96
9	9	18	27	36	45	54	63	72	81	90	99	108
10	10	20	30	40	50	60	70	80	90	100	110	120
11	11	22	33	44	55	66	77	88	99	110	121	132
12	12	24	36	48	60	72	84	96	108	120	132	144

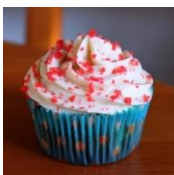
Build on learning from Year 3 and model how grid method and/or expanded method links to compact short multiplication.



$$\begin{array}{r}
 30 + 6 \\
 \times 4 \\
 \hline
 24 \\
 + 120 \\
 \hline
 144
 \end{array}$$

$$\begin{array}{r}
 \phantom{0}^2 36 \\
 \times 4 \\
 \hline
 144
 \end{array}$$

Develop recall of multiplication facts (alongside the inverse of the corresponding division facts).



2 eggs  
150g flour  
180g sugar

Use knowledge of times tables to solve scaling problems.

Susie wants to bake 12 cupcakes people.  
The ingredients given are for four cupcakes.  
How much flour will she need?

	<u>Cupcakes</u>	<u>Flour</u>
	4	150g
x3	12	900g





# Division

## Concrete resources:

Arrays

Multiplication squares

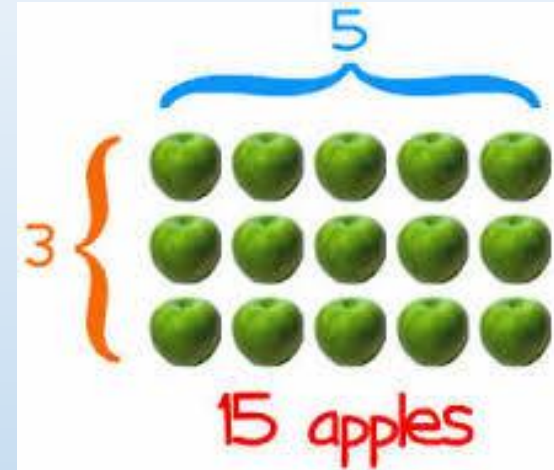
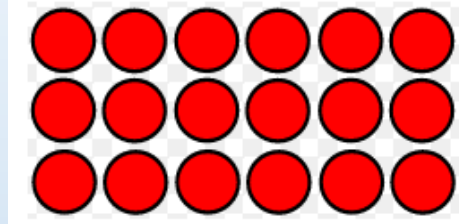
100 square

Number lines

Blank number lines

Counting stick

Place value apparatus



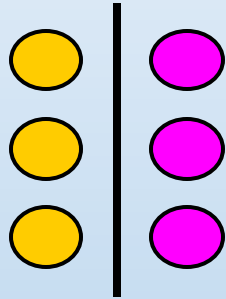
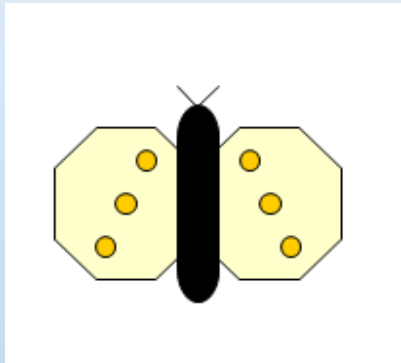
divided by group  
into lots of  $\div$  into groups of  
divisible remainder  
half factor

# Division: Reception

Early learning goal statutory requirement:

✓They solve problems, including halving and sharing.

Use pictorial representations and concrete resources to halve numbers to 10.



Begin to share quantities using practical resources, role play, stories and songs.



**Role play example:**

***It is the end of the party and the final two teddies are waiting for their party bags. Provide empty party bags and a small collection of items such as gifts, balloons and slices of cake. Ask the children to share the objects between the two bags.***

# Division: Year 1

Year 1 statutory requirement:

- solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

Understand division as **sharing** using concrete resources.



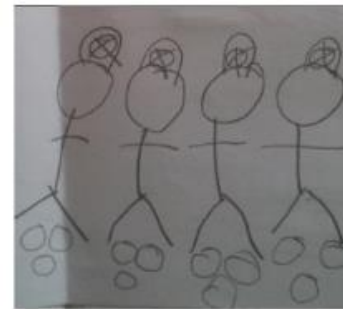
Pictorial representation of sharing **12 gold coins** between 2, 3 and 4 pirates!



$$12 \div 2$$



$$12 \div 3$$



$$12 \div 4$$

Begin to understand division as **grouping** using concrete resources.

12 into groups of 2

$$12 \div 2 = 6$$

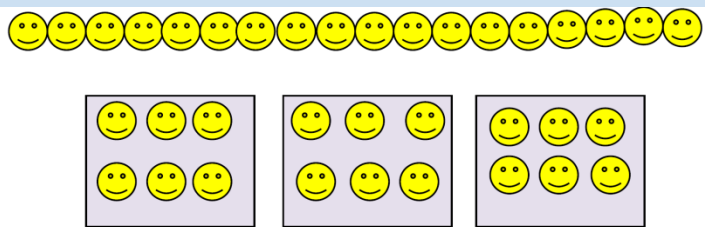


# Division: Year 2

Year 2 statutory requirement:

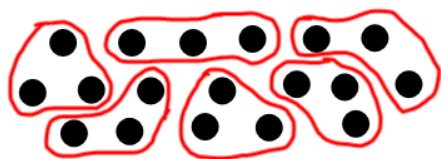
- ✓ Recall and use division facts for 2, 5 and 10 multiplication tables.
- ✓ Calculate mathematical statements for multiplication and division within the multiplication tables and write then using the multiplication (x), division ( ) and equals (=) signs.
- ✓ Solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.
- ✓ **Find  $1/3$ ;  $1/4$ ;  $2/4$ ;  $3/4$  of a length, shape, set of objects or quantity**

Further develop understanding of difference between **sharing** and **grouping** using concrete resources.



18 smiley faces shared between 3 classes.

18 into groups of 3  
 $18 \div 3 = 6$

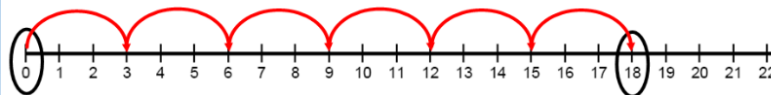


Model division as grouping on a number line (ITP 'Grouping')

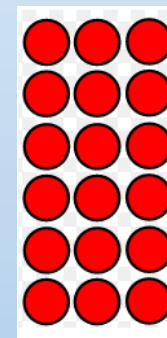


Children use numbered number lines to divide using grouping.

18 into groups of 3 = 6 groups  
18 into jumps of 3 = 6 jumps  
 $18 \div 3 = 6$



Reinforce division through the use of arrays.



$$18 \div 3 = 6$$

$$18 \div 6 = 3$$

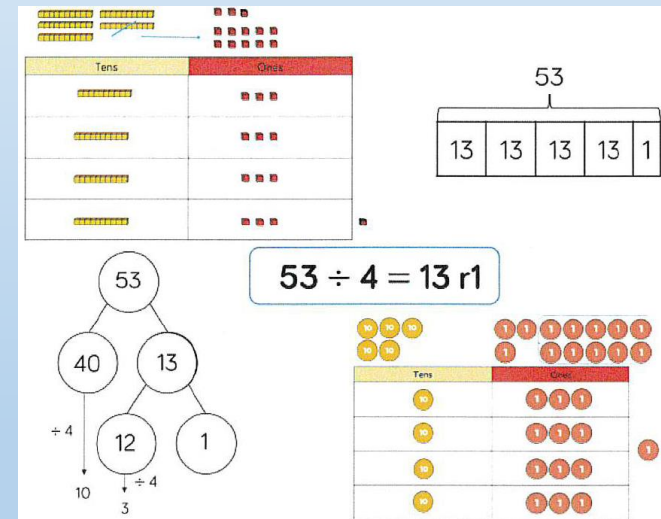
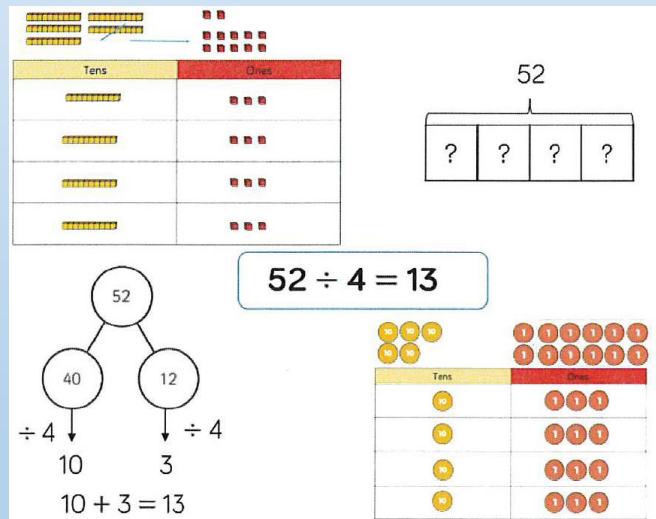
**Remember** to develop connections between fractions and division and rephrase this calculation as  $1/3$  of 18 is the same as  $18 \div 3 = 6$ .

# Division: Year 3 & 4

Year 3 statutory requirement:

- ✓ Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables
- ✓ Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods
- ✓ Solve problems, including missing number problems, involving division including positive integer scaling problems and correspondence problems in which  $n$  objects are connected to  $m$  objects.

Year 4 statutory requirement: **Note** - there isn't a statutory objective for division. However, Y4 statutory multiplication objectives are to (1) recall multiplication and division facts for multiplication tables up to  $12 \times 12$  and (2) multiply two-digit and three-digit numbers by a one-digit number using formal written layout so we will build on the connections between multiplication and division.



**Remember** to develop connections between fractions and division and rephrase these calculations as  $\frac{1}{3}$  of 96;  $\frac{1}{4}$  of 72,  $\frac{1}{4}$  of 872 and  $\frac{1}{5}$  of 185. Note: Year 3 fraction objective - *Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators*; Year 4 fraction objective: *solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number.*

# Division: Year 5

Year 5 statutory requirement:

✓ divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.

Further secure pupils' understanding of compact short division.

$$218 \div 8 =$$
$$27 \text{ r } 2$$
$$8 \overline{)2158}$$

Extend to expressing results in different ways according to the context, including with remainders as fractions, as decimals or by rounding. For example:

- Whole number remainder =  $27 \text{ r } 2$
- Fraction remainder =  $27 \frac{2}{8} = 27 \frac{1}{4}$
- Decimal remainder =  $27 \frac{1}{4} = 27 \frac{25}{100} = 27.25$

# Division: Year 6

Year 6 statutory requirement:

✓ divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context

Continue to use compact short division to divide numbers up to 4 digits by a 1-digit whole number.

$$218 \div 8 =$$
$$27 \text{ r } 2$$
$$8 \overline{) 2158}$$

- Whole number remainder =  $27 \text{ r } 2$
- Fraction remainder =  $27 \frac{2}{8} = 27 \frac{1}{4}$
- Decimal remainder =  $27 \frac{1}{4} = 27 \frac{25}{100} = 27.25$

Use long division to divide numbers up to 4 digits by a 2-digit whole number.

$$24 \overline{) 588}$$
$$\begin{array}{r} 024 \text{ r } 12 \\ - 48 \\ \hline 108 \\ - 96 \\ \hline 12 \end{array}$$

# 2022 End of Key Stage 2 (Year 6)

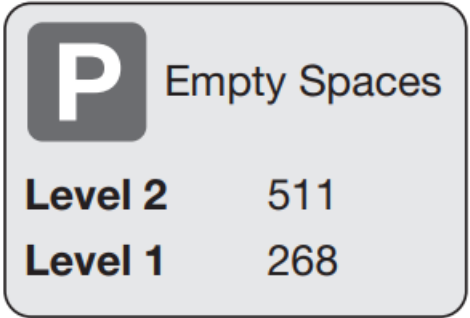
35  $6 + 4 \div 2 =$



1 mark

Arithmetic paper

18 This sign shows the number of **empty spaces** on each level of a car park at 10 am.



Empty Spaces	
Level 2	511
Level 1	268

In this car park, **each** level has 800 spaces.

What is the total number of cars **parked** in the car park at 10 am?

Reasoning paper

# Helping at home

- Count anything and everything (in age appropriate steps forwards and backwards)
- Times tables (Rockstars, songs, games) little and often and include corresponding division facts
- Board games
- Dice games
- Be positive about maths!
- Money/shopping
- Telling the time
- Reading timetables
- Measure – cooking, weighing etc.